## Quadratic inequalities

## A LEVEL LINKS

Scheme of work: 1d. Inequalities - linear and quadratic (including graphical solutions)

## Key points

- First replace the inequality sign by $=$ and solve the quadratic equation.
- Sketch the graph of the quadratic function.
- Use the graph to find the values which satisfy the quadratic inequality.


## Examples

Example 1 Find the set of values of $x$ which satisfy $x^{2}+5 x+6>0$

$$
\begin{aligned}
& x^{2}+5 x+6=0 \\
& (x+3)(x+2)=0 \\
& x=-3 \text { or } x=-2
\end{aligned}
$$

It is above the $x$-axis

1 Solve the quadratic equation by factorising.

2 Sketch the graph of $y=(x+3)(x+2)$

3 Identify on the graph where $x^{2}+5 x+6>0$, i.e. where $y>0$

4 Write down the values which satisfy the inequality $x^{2}+5 x+6>0$

Example 2 Find the set of values of $x$ which satisfy $x^{2}-5 x \leq 0$


1 Solve the quadratic equation by factorising.

2 Sketch the graph of $y=x(x-5)$
3 Identify on the graph where $x^{2}-5 x \leq 0$, i.e. where $y \leq 0$

4 Write down the values which satisfy the inequality $x^{2}-5 x \leq 0$

Example 3 Find the set of values of $x$ which satisfy $-x^{2}-3 x+10 \geq 0$


## Practice

1 Find the set of values of $x$ for which $(x+7)(x-4) \leq 0$

2 Find the set of values of $x$ for which $x^{2}-4 x-12 \geq 0$

3 Find the set of values of $x$ for which $2 x^{2}-7 x+3<0$

4 Find the set of values of $x$ for which $4 x^{2}+4 x-3>0$

5 Find the set of values of $x$ for which $12+x-x^{2} \geq 0$

## Extend

Find the set of values which satisfy the following inequalities.
$6 \quad x^{2}+x \leq 6$
$7 x(2 x-9)<-10$
$8 \quad 6 x^{2} \geq 15+x$

## Answers

$1-7 \leq x \leq 4$
$2 x \leq-2$ or $x \geq 6$
$3 \quad \frac{1}{2}<x<3$
$4 \quad x<-\frac{3}{2}$ or $x>\frac{1}{2}$
$5-3 \leq x \leq 4$
$6-3 \leq x \leq 2$
$72<x<2 \frac{1}{2}$
$8 \quad x \leq-\frac{3}{2}$ or $x \geq \frac{5}{3}$

